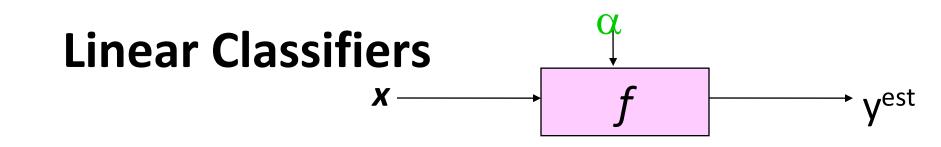


Support Vector Machines

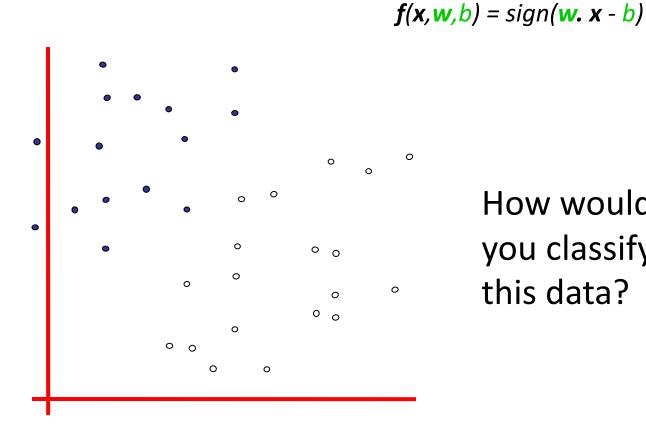
Some slides borrowed from Andrew Moore's <u>slides on SVM</u>s.

Support Vector Machines

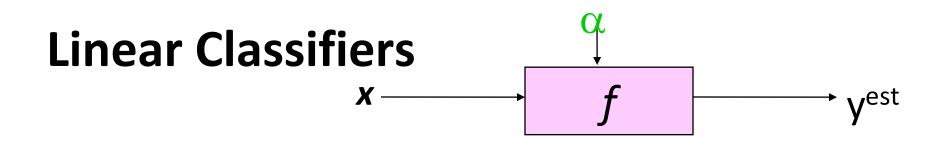
- Popular ML technique
 - -Became popular in the late 90s (Vapnik 1995; 1998)
 - -Invented in the late 70s (Vapnik, 1979)
- Controls complexity and overfitting, so works well on a wide range of practical problems
- Can handle high dimensional vector spaces, which makes feature selection less critical
- Fast and memory efficient implementations, e.g., <u>svm_light</u>
- Not always best solution, especially for problems with small vector spaces



- denotes +1
- denotes -1 0

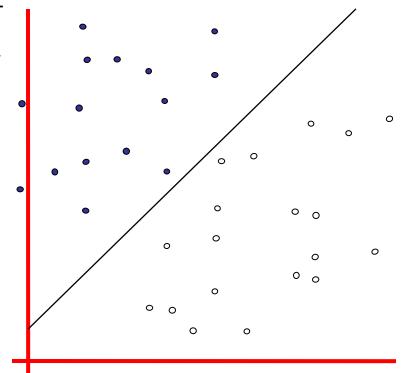


How would you classify this data?



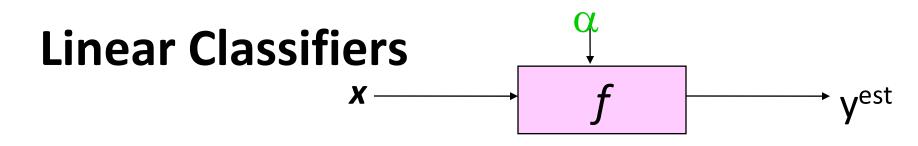
denotes +1

° denotes -1



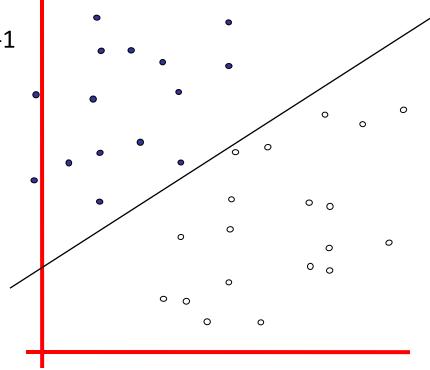
How would you classify this data?

f(x, w, b) = sign(w. x - b)

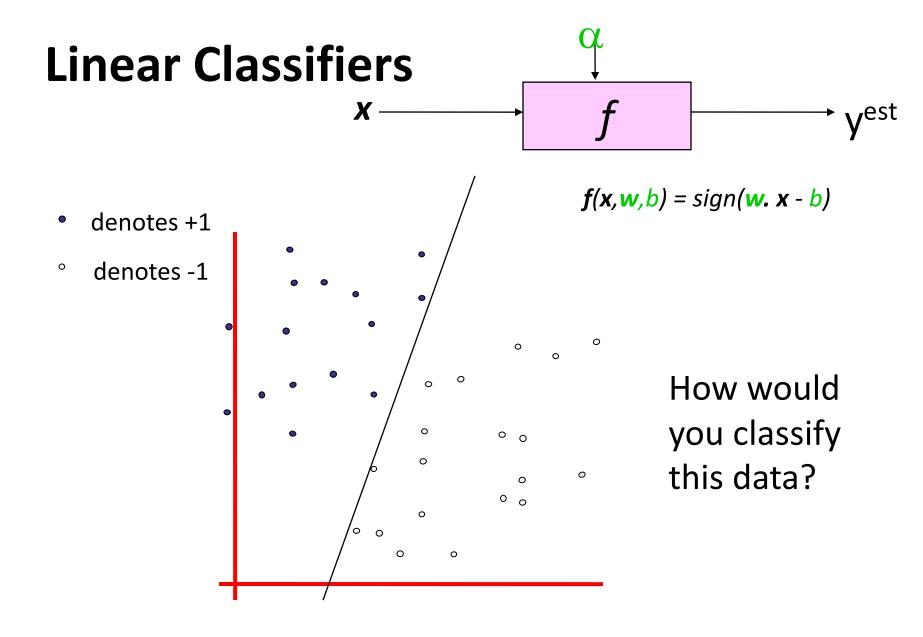


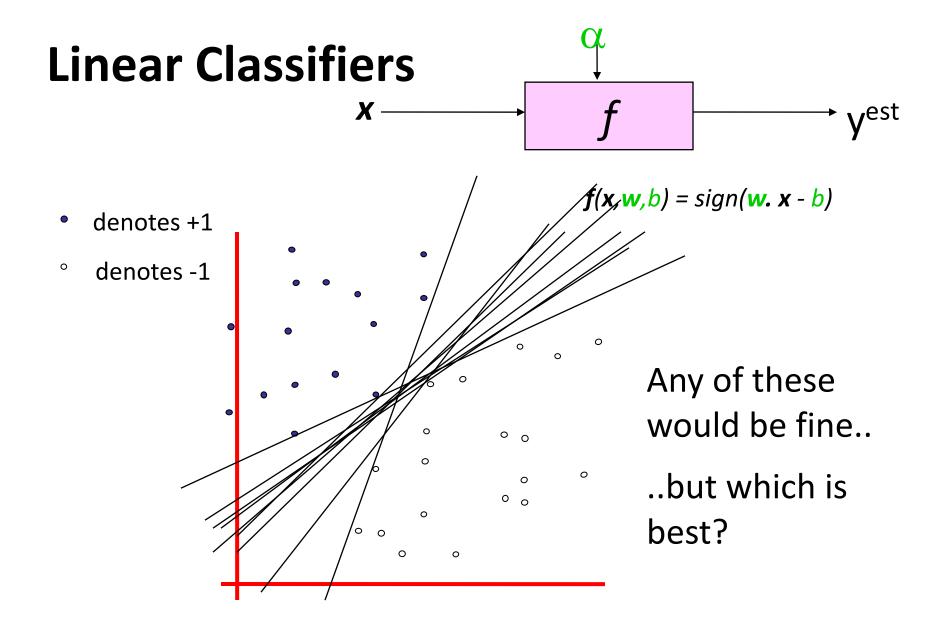
f(**x**, **w**, b) = sign(**w**. **x** - b)

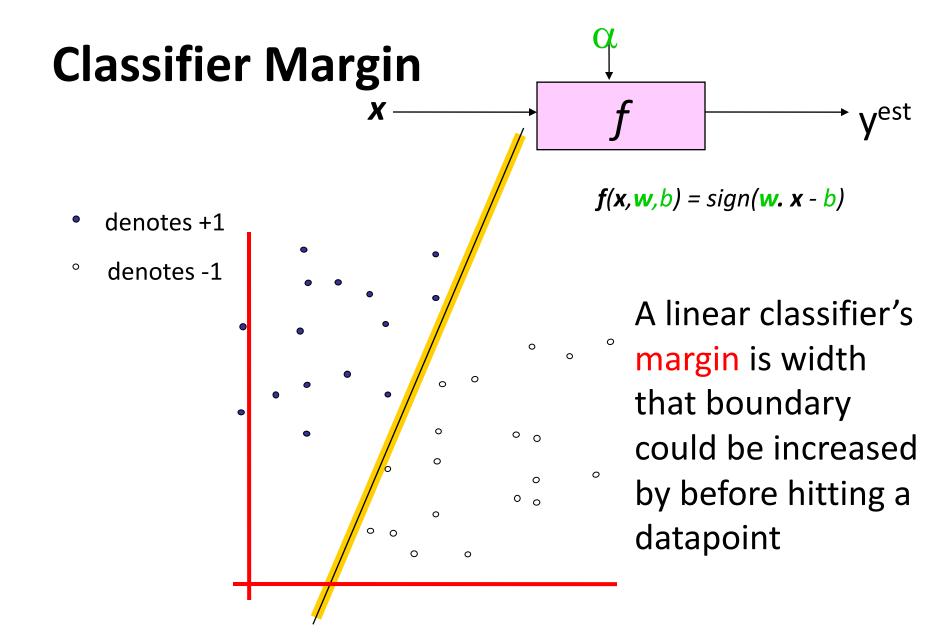
- denotes +1
- ° denotes -1

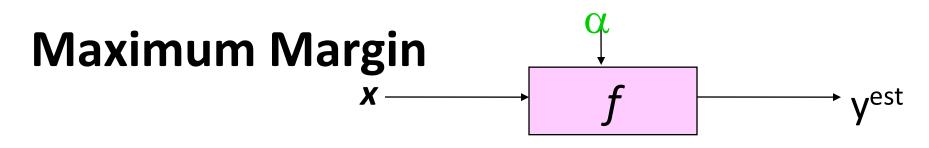


How would you classify this data?

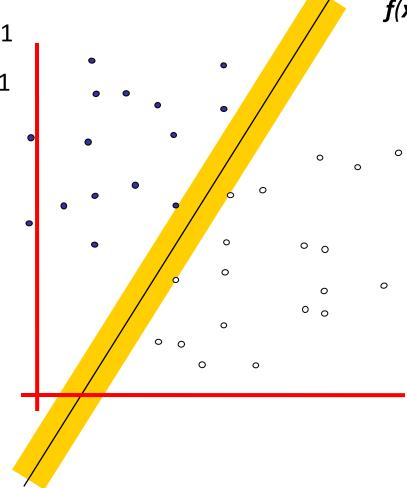








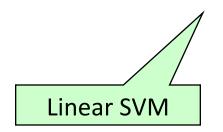
- denotes +1
- ° denotes -1

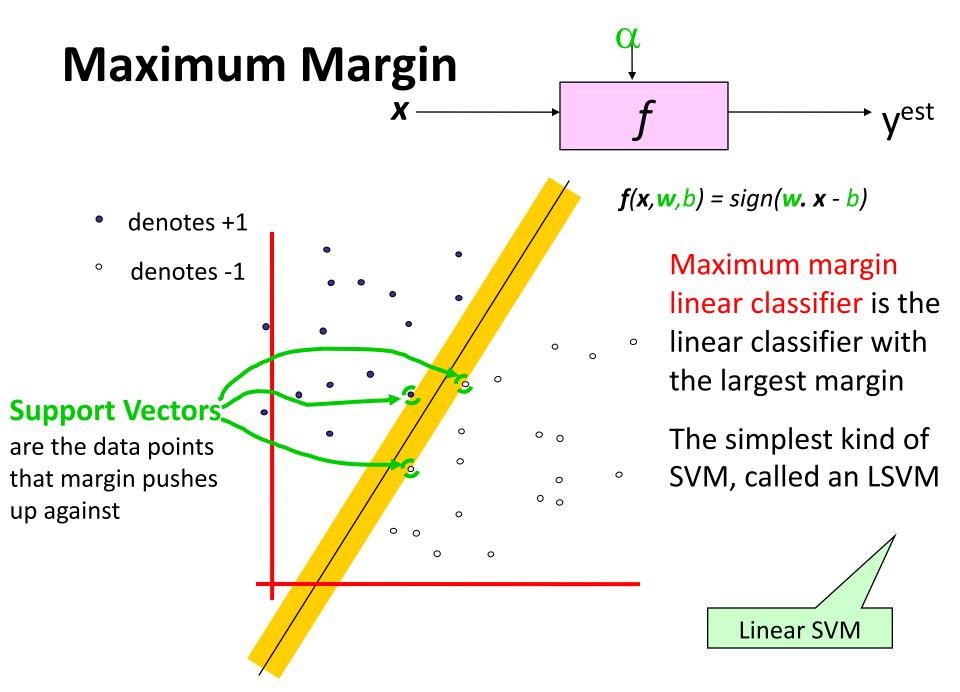


f(**x**, **w**, b) = sign(**w**. **x** - b)

Maximum margin linear classifier is the linear classifier with the largest margin

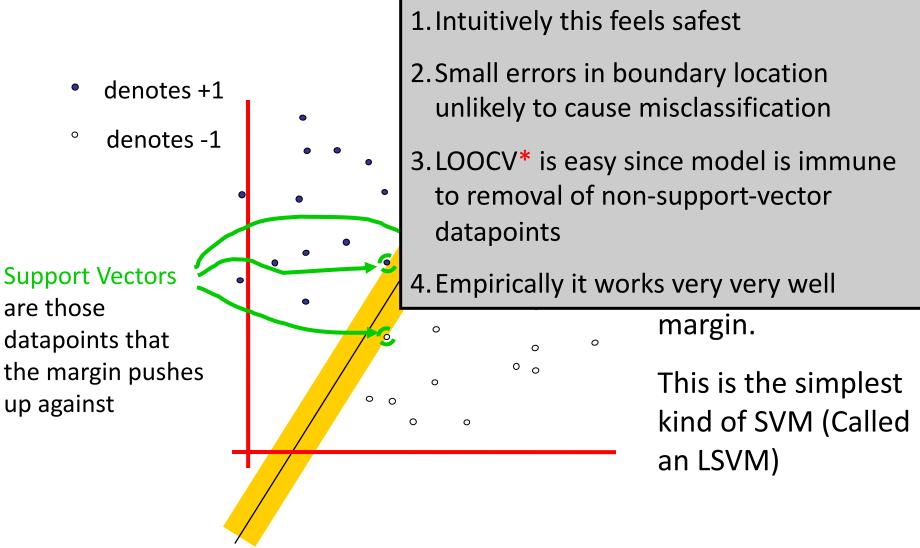
The simplest kind of SVM, called an LSVM





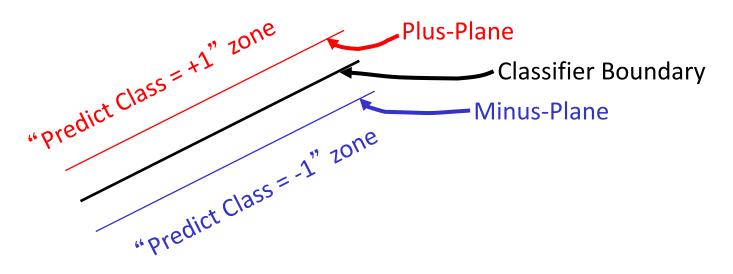
Copyright © 2001, 2003, Andrew W Moore

Why Maximum Margin?



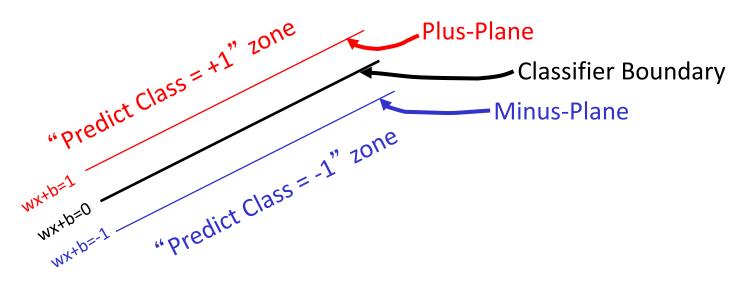
*LOOCV = leave one out cross validation

Specifying a line and margin



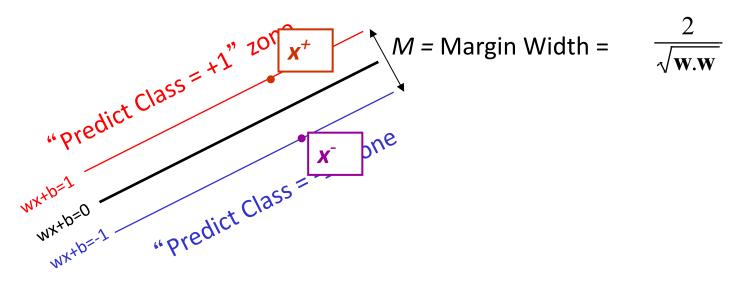
- How do we represent this mathematically?
- ... in *m* input dimensions?

Specifying a line and margin



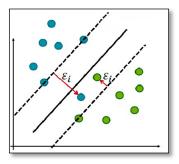
- Plus-plane = { **x** : **w** . **x** + b = +1 }
- Minus-plane = { **x** : **w** . **x** + b = -1 }
 - Classify as.. +1 -1 Universe if $-1 < w \cdot x + b <= -1$ $-1 < w \cdot x + b <= -1$

Learning the Maximum Margin Classifier



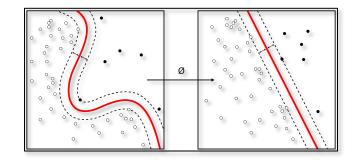
- Given a guess of **w** and b we can
 - Compute whether all data points in the correct half-planes
 - Compute the width of the margin
- Write a program to search the space of **w**s and *b*s to find widest margin matching all the datapoints.
- *How?* -- Gradient descent? Simulated Annealing? Matrix Inversion? EM? Newton's Method?

Soft margin classification



- What if data from two classes not linearly separable?
- Allow a fat decision margin to make a few mistakes
- Some points, outliers or noisy examples, are inside or on wrong side of the margin
- Each outlier incurs a cost based on distance to hyperplane

Kernel trick



- What if data from two classes not linearly separable?
- Project data onto a higher dimensional space where it becomes linearly separable
- Many SVMs can take an argument, a **kernel**, that does the transformation of the data
- Deciding what **kernel function** to use is done through experimentation

Kernel Trick example

Can't separate the blue & red points with a line

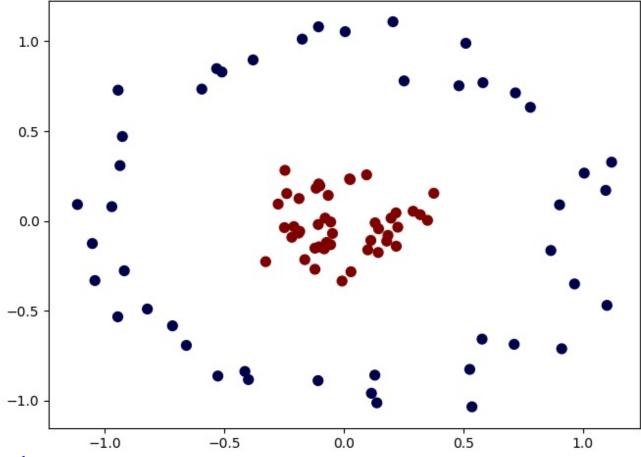
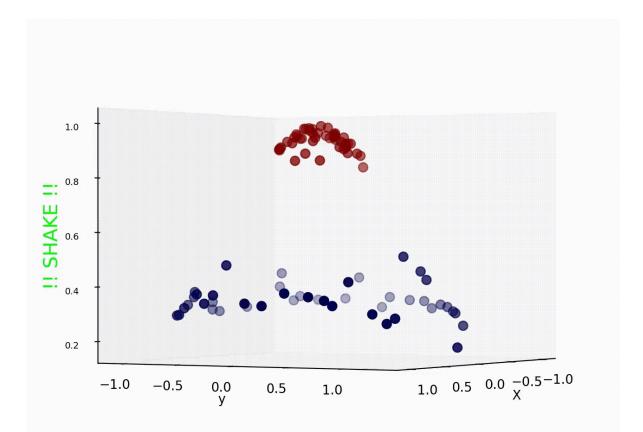


Figure from <u>S. Bhattacharyya</u>

Use a different kernel

- Applying a kernel can transform data to make it more nearly linearly separable
- E.g., use polar coordinates or map to three dimensions



SVM Performance

- SVMs can handle very large features spaces (e.g., 100K features)
- Relatively fast
- Anecdotally they work very well indeed
- Example: They are among the best-known classifier on a well-studied hand-writtencharacter recognition benchmark

100k features?

- SVM used for simple text classification, e.g., classify a text document as
 - expressing sentiment (positive, negative) or political learning (republican, democrat)
- Typically use each word in fixed vocabulary of 25-100k words as a feature/dimension
 - value is TF/IDF number -- frequency of the word in the document relative to all documents
- Product reviews might have ~200 unique words, social media posts only < 20 unique words
- SVMs typically use sparce matrices for efficiency

Binary vs. multi classification

- SVMs only do **binary** classification 😕
 - -E.g.: can't classify an iris into one of three species
- Note: common for many ML classifiers
- Two approaches to multi classification: OVA and OVO
- Consider Zoo dataset, which classifies animals into one of 7 classes based on 17 attributes
 - Classes: mammal, bird, reptile, fish, amphibian, insect, invertebrate
 - Attributes: hair, feathers, eggs, milk, aquatic, toothed, fins, ...

OVA or <u>one-vs-all</u> classification

- OVA or **one-vs-all**: turn n-way classification into n binary classification tasks.
- For zoo problem, train and run 7 binary classifiers:
 - mammal vs. not-mammal
 - fish vs. not-fish
 - bird vs. not-bird, ...
- Pick the one that gives the highest score
 - For an SVM this could be measured the one with the widest margin

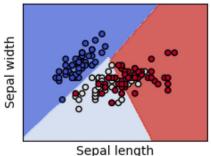
OVO or <u>one vs one</u> classification

- OVO or one vs one: turn n-way classes into N*(N-1)/2 one-vs-one classifiers
 - -mammal vs. bird, mammal vs. reptile ...
 - -bird vs. reptile, bird vs. fish, ...
 - -fish vs. amphibian, fish vs. insect, ...
- Use resulting scores to choose the classification that wins the most 1x1 pairings

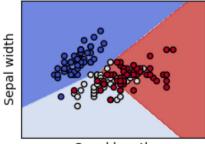
SVMs in scikit-learn

- Scikit-learn has three
 <u>SVM classifiers</u>: SVC, NuSVC, and LinearSVC
- Data can be either in dense numpy arrays or sparse scipy arrays
- All directly support multi-way classification, SVC and NuSCV using OvO and LinearSVC using OvA

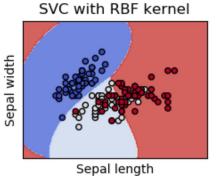
SVC with linear kernel



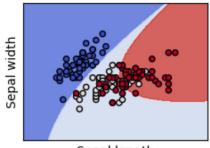
LinearSVC (linear kernel)



Sepal length

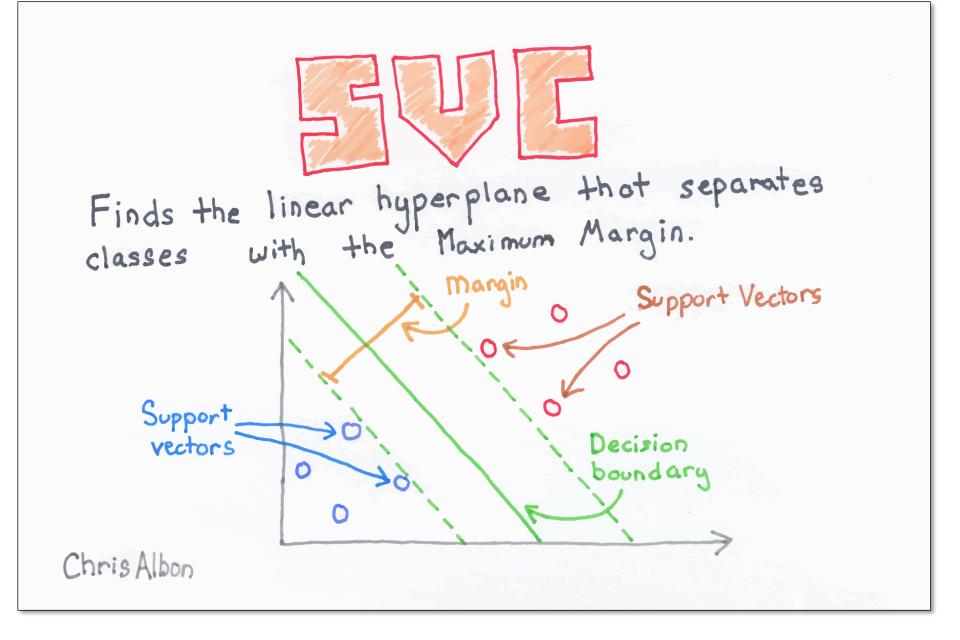


SVC with polynomial (degree 3) kernel



Sepal length

This <u>colab jupyter notebook</u> gets an accuracy of 97% using OvO with <u>scikit.svm.SVC</u>



SVM Summary

- SVM is a good classification technique for problems with a large feature space
- Relatively fast to train and apply the model
- The kernel trick can help make some problems more-nearly linearly separable
- Their binary nature makes then a poorer fit for multi-way classification